Valued Constraint Satisfaction Problem and Resilience in Database Theory

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Dagstuhl Seminar 25211 The Constraint Satisfaction Problem: Complexity and Approximability 22 May 2025



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1/16

Žaneta Semanišinová (TU Dresden) VCSP and Resilience in Database Theory Dagstuhl Seminar, 22 May 2025



2 Complexity results for resilience (new results for digraphs!)



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Definition (resilience)

Fixed conjunctive query q. **Input**: a finite database \mathfrak{A} , $u \in \mathbb{N}$ **Output**: Can we remove $\leq u$ tuples from relations of \mathfrak{A} , so that $\mathfrak{A} \not\models q$?

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Example: The resilience of

$$q = \exists x, y, z(R(x, y) \land R(y, z))$$

with respect to \mathfrak{A} is 1 - remove (C, E).



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Goal: Classify complexity of resilience for all *q*.

Example: $q := \exists x, y (R(x, y) \land S(y))$ $R \xrightarrow{S} R(x,y) \xrightarrow{Y} R(x,y) \xrightarrow{$



• \mathfrak{B}_q can be chosen so that $\operatorname{Aut}(\mathfrak{B}_q)$ is oligomorphic.

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$$\frac{R}{x} \frac{S}{y}$$

canonical structure incidence graph I(q)

R(x, y) = S(y)

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Theorem (Cherlin, Shelah, Shi '99)

Let q be a query and \mathfrak{Q} its canonical structure. If I(q) is connected, then there exists a dual structure \mathfrak{B}_q , such that for every finite \mathfrak{A} :

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- \mathfrak{B}_q can be chosen so that $\operatorname{Aut}(\mathfrak{B}_q)$ is oligomorphic.
- B_q can be chosen finite iff q is homomorphically equivalent to q' such that l(q') is a tree. (Nešetřil, Tardiff '00; Larose, Loten, Tardiff '07)

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oligomorphic – countable domain B_q and the action of $Aut(\mathfrak{B}_q)$ on B_q^n has finitely many orbits for every $n \ge 1$

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Example: For every finite directed graph *G* we have:

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Input: a finite database \mathfrak{A} , $u \in \mathbb{N}$

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More flexible approach: valued CSPs

Valued CSPs

A valued structure Γ consists of:

- (countable) domain C
- (finite, relational) signature au
- for each $R \in \tau$ of arity k, a function $R^{\Gamma}: C^k \to \mathbb{Q} \cup \{\infty\}$

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Definition (VCSP(Γ))

Input: $u \in \mathbb{Q}$, an expression

$$\phi(x_1,\ldots,x_n)=\sum_i\psi_i,$$

where each ψ_i is an atomic τ -formula **Question:** Is

$$\inf_{t\in C^n}\phi(t)\leq u \text{ in } \Gamma?$$

Input: G = (V, E) – finite directed (multi)graph **Goal**: Find a partition $A \cup B$ of V such that $E \cap (A \times B)$ is maximal. Equivalently: $E \cap (A^2 \cup B^2 \cup B \times A)$ is minimal.

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Let Γ_{MC} be a valued structure where:

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$$C = \{a, b\}$$

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$$\tau = \{R\}$$
, R binary

$$R(x,y) = \begin{cases} 0 \text{ if } x = a \text{ and } y = b \\ 1 \text{ otherwise} \end{cases}$$



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Take vertices of G as variables. The size of a maximal cut of G is

 $\min_{x \in C^n} \sum_{(x_i, x_j) \in E} R(x_i, x_j).$ The partition of V is given by the values a and b.

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every instance of VCSP(Γ_{MC}) corresponds to a directed multigraph $\sim VCSP(\Gamma_{MC})$ is the Max-Cut problem (NP-hard)

Connection of resilience and VCSPs

query q (WLOG I(q) connected) \rightarrow dual $\mathfrak{B}_q \rightarrow 0$ -1-valued structure Γ_q Example:



resilience of $q = VCSP(\Gamma_{MC}) = Max-Cut$ is NP-hard

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Theorem (Bodirsky, S., Lutz '24)

The resilience problem for q equals $VCSP(\Gamma_q)$.

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Remark: We have to consider bag databases – a database \mathfrak{A} might contain a tuple with multiplicity > 1 (differs from the original setting). **Example:** Input R(x, y) + R(x, y) for VCSP(Γ) corresponds to a database with multiplicity 2 for R(x, y).

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Theorem

For a finite-domain valued structure Γ , VCSP(Γ) is in P or NP-complete.

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Let q be a conjunctive query such that I(q) is acyclic. Then the resilience problem for q is in P or NP-complete.

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Question: For general queries, choose \mathfrak{B}_q with oligomorphic Aut (\mathfrak{B}_q) . Can we use adapt some results for finite domains?

Definition

Let Γ and Δ be valued τ -structures with domains C and D, respectively. A fractional homomorphism from Δ to Γ is a probability distribution ω on the maps $f: D \to C$ such that for every k-ary $R \in \tau$ and tuple $t \in D^k$

 $E_{\omega}[f \mapsto R^{\Gamma}(f(t))] \leq R^{\Delta}(t).$

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Special cases:

- fractional endomorphism if $\Delta = \Gamma$
- Dirac fractional homomorphism if $\omega(f) = 1$ for some $f: D \to C$

 $\Gamma^{\ell} = (C^{\ell}; (R^{\Gamma^{\ell}})_{R \in \tau})$ where

$$R^{\Gamma^\ell}((t_1^1,\ldots,t_\ell^1),\ldots,(t_1^k,\ldots,t_\ell^k)):=rac{1}{\ell}\sum_{i=1}^{\iota}R^{\Gamma}(t_i^1,\ldots,t_i^k).$$

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Theorem (Bodirsky, S., Lutz '24)

If Γ_q has a fractional polymorphism which is canonical and pseudo cyclic, then VCSP(Γ_q) is in *P*.

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 → analogy of pp-definable relations

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- K_3 complete graph on 3 vertices, viewed as a 0- ∞ valued structure

Proposition (Bodirsky, S., Lutz '24)

If Aut(Γ) is oligomorphic and Γ pp-constructs K_3 , then VCSP(Γ) is NP-hard.

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Proposition (Bodirsky, S., Lutz '24)

If $Aut(\Gamma)$ is oligomorphic and Γ pp-constructs K_3 , then $VCSP(\Gamma)$ is NP-hard.

Conjecture: If Γ_q does not pp-construct K_3 , then the tractability theorem applies and VCSP(Γ_q) and hence resilience of q is in P.

Resilience for digraphs

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$$q_c := \exists x, y \ R(x, y)R(y, x)$$

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Theorem (Bodirsky, S. '25)

Let q be a minimal connected conjunctive query over the signature $\{R\}$. Then either q is equal to q_{ℓ} , q_1 or q_c and the resilience of q is in P, or the resilience problem of q is NP-complete. R – binary relation symbol

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Conjecture: NP-hardness always comes from pp-constructing K_3 .

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Theorem (Bodirsky, Jahel, S. '25)

Let Γ be a valued structure such that all of its valued relations attain values from $\{0, 1, \infty\}$. Then there exists a valued core Δ with Aut (Δ) oligomorphic such that:

- Δ is a substructure of Γ ;
- Γ and Δ are fractionally homomorphically equivalent and the fractional homomorphisms can be chosen to be Dirac;
- every valued core which is frac. hom. equiv. to Γ is isomorphic to Δ .

Fact: Γ pp-constructs K_3 if and only if its underlying crisp structure does.

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Question: Can the results on valued cores be generalized to all valued structures with an oligomorphic automorphism group?

Thank you for your attention

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